



## MECÂNICA ESTRUTURAL – 10371/10391/10411

2014/2015

### Assignment 1

#### OBJECTIVES

To learn how to implement a computer code to solve a structural problem, using the finite element method.

#### 1. PROBLEM

A wing spar of an ultralight aircraft is to be sized for minimum weight using the finite element method. In the finite element formulation of the Euler-Bernoulli beam, assume that the cross-section properties are constant within the element. Determine the width,  $b$ , and thickness,  $t = t_0 + t_1 \cdot x$ , of the wing's cross-section for minimum weight subject to a maximum tip deflection of 10% of the semi-span,  $L$ ; a safety factor of  $FS = 1.5$  and a minimum safety margin in any position along the spar of  $MS = 0.2$ . Assume that  $b \leq h$ .

Plot the transverse deflection,  $w$ , the rotation,  $\theta$ , the thickness,  $t$ , the maximum stress,  $\sigma$ , and the safety margin,  $MS$ , as functions of the position,  $x$ , along the spar.

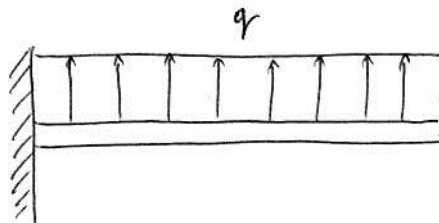
#### 2. DATA

Each group should select a different combination of loading, cross-section and material from the options below.

Material		
i	Young's modulus	$E = 70 \text{ GPa}$
	Ultimate direct stress	$\sigma_{\max} = 600 \text{ MPa}$
ii	Young's modulus	$E = 100 \text{ GPa}$
	Ultimate direct stress	$\sigma_{\max} = 1000 \text{ MPa}$

### Loading

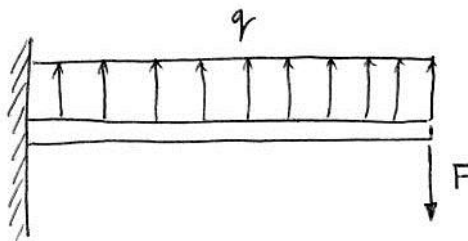
1



$$L = 5 \text{ m}$$

$$q = 1800 \text{ N/m}$$

2

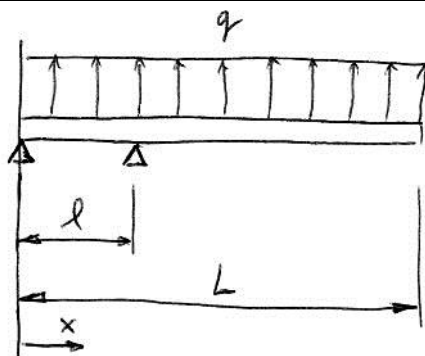


$$L = 5 \text{ m}$$

$$q = 1800 \text{ N/m}$$

$$F = 250 \text{ N}$$

3



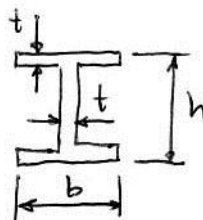
$$L = 5 \text{ m}$$

$$l = 2 \text{ m}$$

$$q = 1800 \text{ N/m}$$

### Cross-section

A



$$h = 0.1 \text{ m}$$

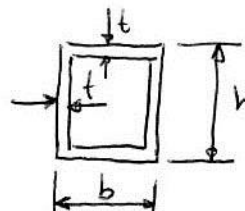
$$b = ?$$

$$t = t_0 + t_1 * x$$

$$t_0 = ?$$

$$t_1 = ?$$

B



$$h = 0.1 \text{ m}$$

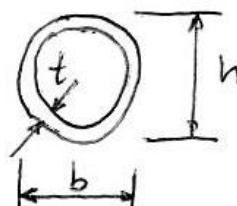
$$b = ?$$

$$t = t_0 + t_1 * x$$

$$t_0 = ?$$

$$t_1 = ?$$

C



$$h = 0.1 \text{ m}$$

$$b = ?$$

$$t = t_0 + t_1 * x$$

$$t_0 = ?$$

$$t_1 = ?$$